

In the second formula the number is written as $x = +$

Example write the following numbers in the floating point formula and three decimal places

$$x = 63249 = 0.63249 = 0.632 + 0.49$$

$$Y = -1579.26 = -0.157926 = -0.157 + (-0.926)$$

$$z = 0.01295 = 0.1295 = 0.129 + 0.5$$

$$k = 173.18 = 0.17318 = 0.173 + 0.18$$

Finding the absolute and relative errors

1) Errors in chopping case

Let $x = +$, =

$$(x) = = = =$$

$$(x) = =$$

$$(x) =$$

$$(x) = =$$

2) Errors in chopping case

Let $x = + , =$

+

$(x) = = =$

$(x) = = =$

$(x) = = = = 0.5$

$(x) = = =$

Fundamental theorem of algebra

Every polynomial of degree n has n roots in complex numbers

Let f be a continuous function on $[a, b]$

If $f(a) f(b) < 0$ then there exists roots in $[a, b]$

If $f(a) f(b) > 0$ then there is no roots in $[a, b]$

Example Find the position of roots of $f(x) = -x^2 + 3x - 10$ in $[-8, 8]$

x	-8	-6	-4	-2	0	2	4	6	8
F(x)	+	+	+	+	-	+	-	+	+

$f(-2) f(0) < 0$ then there exists roots in $[-2, 0]$

$f(0) f(2) < 0$ then there exists roots in $[0, 2]$

$f(2) f(4) < 0$ then there exists roots in $[2, 4]$

$f(4) f(6) < 0$ then there exists roots in $[4, 6]$

1) Bisection methods

Example Find the root of $x =$ in $[0,1]$

$$F(x) = x -$$

$$F(0) = -1, f(1) = 0.632$$

$f(0) f(1) < 0$ then there exists roots in $[0, 1]$

$$= (0+1)/2 = 0.5, f(0.5) = -0.1065$$

$f(0) f(0.5) > 0$ then there is no roots in $[0, 0.5]$

$f(0.5) f(1) < 0$ then there exists roots in $[0.5, 1]$

$$= (0.5+1)/2 = 0.75, f(0.75) = 0.2776$$

$f(0.75) f(1) > 0$ then there is no roots in $[0.75, 1]$

$f(0.5) f(0.75) < 0$ then there exists roots in $[0.5, 0.75]$

$$= (0.5+0.75)/2 = 0.625, f(0.625) = 0.0897$$

$f(0.625) f(0.75) > 0$ then there is no roots in $[0.625, 0.75]$

$f(0.5) f(0.625) < 0$ then there exists roots in $[0.5, 0.625]$